CHROM. 22 238

# **Calculation of programmed temperature gas chromatographic characteristics from isothermal data**

# **III. Predicted retention indices and equivalent temperatures**

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# SUMMARY

Theoretical procedures, described in Part I [J. *Chromutogr., 405 (1987) 671,* for predicting retention indices in programmed temperature gas chromatography from isothermal data are experimentally tested for a number of compounds under a range of experimental conditions. In general, and taking into full consideration random error predictions, agreement is reasonably satisfactory. Also calculated by procedures of Part I are two distinct kinds of equivalent temperature, these being the temperatures of isothermal chromatographic experiments giving the same calculated retention time (a) or index (b) as a corresponding programmed temperature experiment. These temperatures are compared with various simple functions of initial and calculated final temperatures in such an experiment.

# INTRODUCTION

Part  $I<sup>1</sup>$  describes theoretical and computational procedures for predicting programmed-temperature gas chromatography (PTGC) characteristics using, as input information, experimental data for the same column and carrier gas pressure differential, but obtained under isothermal conditions (isothermal gas chromatography, IGC). Part  $II^2$  describes the calculation (with due consideration of random errors), and comparison with experiment, of retention times and elution temperatures for a range of organic compounds (n-alkanes, monocyclic aromatic hydrocarbons and ketones) on a capillary column under a variety of programmed-temperature conditions; the temperature programme corresponded in each case to a linear increase of temperature with time ("single linear ramp"). The present paper extends the comparison to PTGC retention indices and also calculates two kinds of equivalent

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temperature'. These are the temperatures of IGC experiments for which, on the one hand, retention times are the same as calculated PTGC values, and on the other hand, retention indices are the same. The equivalent temperatures are then compared with various averages of initial and elution temperatures and with the Giddings significant temperature<sup>3</sup>.

## EXPERIMENTAL

The experimental procedure is fully described in Part  $II^2$ , which also lists the compounds studied. The list is repeated in the first column of Tables I and II. For the present purpose, it should be noted that it includes a contiguous set of n-alkanes, to be used as retention index standards for the remaining compounds.

# PREDICTED EQUIVALENT TEMPERATURES (RETENTION TIME TYPE)

Part  $II<sup>2</sup>$  presents (a) experimental isothermal retention times for the compounds studied, (b) two simple alternative relationships between column dead time and

# TABLE I

PREDICTED EQUIVALENT TEMPERATURES (RETENTION TIME TYPE) AND VARIOUS TRADI Values in parentheses are estimated standard deviations.



a Values are given in the order (a) arithmetic mean of initial and calculated elution temperature, (b) corresponding harmonic mean, (c) Giddings significant temperature, *i.e.,* 0.92 x calculated elution temperature.

temperature derived from the values of (a) for  $n$ -alkanes, (c) least squares linear regression coefficients for plots of ln(capacity factor) against reciprocal absolute temperature, and (d) a selection of predicted PTGC retention times and elution temperatures for a variety of single-linear-ramp programmed conditions using the theoretical/computational procedures described in Part  $I^1$ . From this starting point, one can calculate' the temperatures of corresponding IGC experiments predicted to have the same retention times as the PTGC experiments; in Part I, such an "equivalent temperature" has been symbolised  $T_{eq(1)}$ . Tables I and II give a selection of these, together with estimates of standard deviations derived from a numerical application of error propagation theory<sup>1,2</sup>.

Because of the close similarity in predictions using two alternative column dead time formulae' (and this is also the case in the predictions of Part II), these and subsequent tables in this paper have been restricted to predictions from one of the formulae, *viz.,* 

$$
t/\text{s} = -46.4(3.6) + 6.54(0.179)\sqrt{T/\text{K}}; \text{covariance} - 0.64 \tag{1}
$$

where t is the column dead time at absolute temperature  $T$  (in this paper standard

# TIONAL EQUIVALENT TEMPERATURES FOR HEATING RATE OF 2.00 AND 7.00 K min-'



# TABLE II

#### PREDICTED EQUIVALENT TEMPERATURES (RETENTION TIME TYPE) AND VARIOUS TRADI-TIONAL EQUIVALENT TEMPERATURES FOR HEATING RATE OF  $15.00 \text{ K min}^{-1}$

Values in parentheses are estimated standard deviations.



a Values are given in the order (a) arithmetic mean of initial and calculated elution temperature, (b) corresponding harmonic mean, (c) Giddings significant temperature, *i.e.*,  $0.92 \times$  calculated elution temperature.

deviations are given in parentheses). A full set of data covering both formulae and 32 combinations (listed in Part II) of initial oven temperature and heating rate is available from the authors on request. Also included in Tables I and II, for comparison purposes, are the arithmetic and harmonic means of initial and *calculated* elution temperatures and the *calculated* Giddings significant temperature (0.92  $\times$  calculated elution temperature)<sup>3</sup>, all three of which have been used in the past as "equivalent" temperatures".

PREDICTED PTGC RETENTION INDICES AND EQUIVALENT TEMPERATURES (RETEN-TION INDEX TYPE)

For the same selection of experimental conditions, Tables III-V give calculated retention indices by two alternative procedures, (a) by linear interpolation between adjacent points on a plot of programmed temperature retention time against carbon number for *n*-alkanes, and (b) by cubic spline interpolation for the same plot (the two methods are detailed in Part  $I^1$ ). Observed values corresponding to the calculated values of method (b) are included for comparison. The tables also present calculated

#### TABLE III

PREDICTED AND OBSERVED RETENTION INDICES AND EQUIVALENT TEMPERATURES (RETENTION INDEX TYPE) FOR INITIAL TEMPERATURES OF 333.16 AND 393.16 K AND A HEATING RATE OF  $2.00 \text{ K} \text{ min}^{-1}$ 

For each compound, the first and second lines correspond to initial temperatures of 333.16 and 393.16 K, respectively.



<sup>a</sup> Values in parentheses are estimated standard deviations. Retention index (a)<sup>1</sup> is obtained by linear interpolation between adjacent points on a plot of programmed temperature retention time against carbon number for *n*-alkanes. Retention index (b)<sup>1</sup> is obtained by cubic spline interpolation for the same plot. Equivalent temperature  $(a)^1$  uses retention index  $(a)$  in conjunction with a linear interpolation between adjacent points on a plot of log(isothermal capacity factor) against carbon number for  $n$ -alkanes. Equivalent temperature  $(b)^1$  uses retention index (b) in conjunction with a least squares linear fit to the points of the same plot.

<sup>b</sup> Values in parentheses are 95% confidence deviations. Experimental values are analogues of the predicted indices (b).

temperatures of IGC experiments for which Kováts retention indices are the same as calculated PTGC indices; in Part I, such an "equivalent temperature" has been symbolised  $T_{eq(2)}$ . Again two different methods have been used to calculate these: method (a) uses retention index (a) in conjunction with a linear interpolation between adjacent points of a plot of log(isotherma1 capacity factor) against carbon number for  $n$ -alkanes; method (b) uses retention index (b) in conjunction with a least squares linear fit to the points of the same plot. Standard deviation estimates (see Part  $I^1$ ) are included for all calculated values.

#### TABLE IV

# PREDICTED AND OBSERVED RETENTION INDICES AND EQUIVALENT TEMPERATURES (RETENTION INDEX TYPE) FOR INITIAL TEMPERATURES OF 333.16 AND 339.16 K AND A HEATING RATE OF 7.00 K min<sup>-1</sup>

For each compound, the first and second lines correspond to initial temperatures of 333.16 and 393.16 K, respectively



 $a,b$  See corresponding footnotes for Table III.

# DISCUSSION

Corresponding PTGC retention indices calculated by the two methods are very similar; in the main, bearing in mind the estimated standard deviations, they may indeed be regarded as indistinguishable. Agreement between predicted and observed is generally good, again in the light of the stated uncertainties, although there is certainly a tendency for observed values to be higher. The situation is shown graphically in Fig. 1, which excludes any error considerations; the compound to box number correspondence is given in Table III. It will be seen that for four compounds predictions are less satisfactory than for the others. These four are nonan-5-one (compound 1) where predictions are *consistently* high, and valerophenone, hexanophenone and 1-phenyloctane (compounds 4,5 and 11) where there is significant spread of predictions around the observations. Possible reasons for imperfect prediction have been presented in Part

#### TABLE V

PREDICTED AND OBSERVED RETENTION INDICES AND EQUIVALENT TEMPERATURES (RETENTION INDEX TYPE) FOR INITIAL TEMPERATURES OF 333.16 AND 393.16 K AND A HEATING RATE OF 15.00 K min-'

For each compound, the first and second lines correspond to initial temperatures of 333.16 and 393.16 K, respectively.



 $a,b$  See corresponding footnotes for Table III.

II<sup>2</sup>. Predictions based upon similar theory by Curvers *et al.*<sup>4</sup> (but without any error considerations) are rather closer to their experimental values than those given here.

Because both predicted elution temperatures' and predicted retention indices generally compare well with experiment, it may be supposed that comparison of *calculated* equivalent temperatures (both types) and *calculated* "comparison temperatures" (three kinds as given in Tables I and II) corresponds reasonably closely with comparison of *experimental* values. The difference in nature between the two types of equivalent temperature [retention time type  $T_{eq(1)}$  (Tables I and II) and retention index type  $T_{\text{eq}(2)}$  (Tables III–V)] has been emphasised in Part I<sup>1</sup>. Comparison of values for corresponding eluent and PTGC conditions certainly indicate significant differences in many cases. Furthermore, there are some significant differences between values of  $T_{eq(2)}$  calculated by the two different methods; incidentally, the generally higher estimated standard deviations by method (b) arise from the involvement of *all*   $n$ -alkanes [in contrast with only two for method (a)] in the linear regression aspect of



Fig. 2. Test of arithmetic mean of initial and experimental elution temperature as an approximator of  $T_{\text{eq},2}$  for propiophenone:  $\Delta =$  IGC retention index vs 1000 for hexanophenone and 1-phenyloctane, the arrowed points are those for the former compound. The point symbols correspond to the pairs of initial temperatures/K and heating rates/K min<sup>-1</sup> as follows:  $\Delta = 333.16$ ,  $2.00$ ;  $\nabla = 393.16$ ,  $2.00$ ;  $+ = 333.16$ ,  $7.00$ ;  $\overline{C} = 333.16$ ,  $15.00$ ;  $\overline{O} = 393.16$ ,  $15.00$ .

K/isothermal temperature;  $\nabla + \times \Box$  = experimental PTGC retention index vs. 1000 K/arithmetic mean temperature for initial temperatures of 333.16, 353.16, 373.16 and 393.16 K, respectively. For each temperature, points from the bottom of the line upwards are for heating rates of 1.00, 2.00, 3.00, 3.00, 7.00, 10.00, 12.00 and  $15.00 K min^{-1}$ .

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#### TABLE VI

CALCULATED EQUIVALENT TEMPERATURES (RETENTION INDEX TYPE) FOR HYPO-THETICAL COMPOUND

 $ln(k_1) = -12.2 (0.02), k_2 = 5000 (10)$  K, covariance -0.2. Column dead time/temperature dependence as eqn. 1; initial temperature =  $333.16$  K.



the method. There is certainly a possibility of ill-conditioning in the calculation of  $T_{eq(2)}$  in situations where the IGC (Kováts) indices are only very slightly dependent on temperature. To illustrate this, a hypothetical example [for which<sup>1</sup>  $ln(k_1) = -12.2$ (0.02) and  $k_2$  = 5000 (10) K; covariance = -0.2;  $\ln(k_1)$  and  $k_2$  are the intercept and slope, respectively, of the least squares linear plot of In (isothermal capacity factor) against reciprocal absolute temperature] gave the absurd results shown in Table VI; at least in this example, there is more "stability" in  $T_{eq(2)}$  values obtained by method (b).

In comparing both  $T_{eq(1)}$  (all compounds) and  $T_{eq(2)}$  (inapplicable for the n-alkanes) with the various comparison temperatures given in Tables I and II, it is apparent that *generally* (and there are exceptions) (i) neither equivalent temperature compares well with the Giddings significant temperature, (ii)  $T_{eq(1)}$  compares better with one or other of the means of initial and elution temperatures than does  $T_{eq(2)}$ . The quality of various comparison temperatures as approximators of  $T_{eq(2)}$  has been previously<sup>5</sup> approached in a different way, viz., by plotting experimental IGC retention indices against reciprocal absolute temperature (this being nearly linear, and equivalent to a plot of PTGC index against experimental  $T_{eq(2)}^{-1}$ ), and then examining the proximity of points [(experimental comparison temperature) $^{-1}$ , experimental PTGC index] to the plot; the closer the points, the better the comparison temperature as an approximator of  $T_{eq(2)}$ . This approach is illustrated in Figs. 2-4 for propiophenone; experimental IGC indices at 393.16, 403.16, 413.16 and 423.16 K are 1178.1, 1181.7, 1185.8 and 1189.8, respectively. Generally, and this is particularly true at



Fig. 3. Test of harmonic mean of initial and experimental elution temperature as an approximator of  $T_{eq,2}$ for propiophenone:  $\triangle$  = IGC retention index vs. 1000 K/isothermal temperature;  $\nabla$  +  $\times$   $\square$  = experimental PTGC retention index vs. 1000 K/harmonic mean temperature for initial temperatures of 333.16, 353.16, 373.16 and 393.16 K, respectively. For each temperature, points from the bottom of the line upwards are for heating rates of 1.00, 2.00, 3.00, 5.00, 7.00, 10.00, 12.00 and 15.00 K min<sup>-1</sup>.

Fig. 4. Test of Giddings significant temperature as an approximator of  $T_{\text{eq},2}$  for propiophenone:  $\triangle$  = IGC retention index vs 1000 K/isothermal temperature;  $\nabla + \times \Box$  = experimental PTGC retention index vs. 1000 K/Giddings significant temperature for initial temperatures of 333.16, 353.16, 373.16 and 393.16 K, respectively. For each temperature, points from the bottom of the line upwards are for heating rates of 1.00, 2.00, 3.00, 5.00, 7.00, 10.00, 12.00 and 15.00 K min<sup>-1</sup>.

higher initial column initial temperatures, the arithmetic mean (and to a slightly lesser extent the harmonic mean) is a better  $T_{eq(2)}$  approximator than is the Giddings significant temperature. The same tendency applies for other eluents.

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